



POLITECHNIKA POZNAŃSKA

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Basics of Smart Systems exercise 1

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Exercise 1.1

There is a unipolar sigmoidal activation function

$$\varphi(v) = \frac{1}{1 + e^{-av}}, \quad a > 0,$$

Find asymptotes of functions; what is the value of the function for $v=0$?

Find derivative of function, prove that

$$\varphi'(v) = \frac{d\varphi(v)}{dv} = a\varphi(v)[1 - \varphi(v)]$$

What is the value of $\varphi'(0)$?

Draw a graph of the function

Exercise 1.2

Activation function is defined by formula

$$\varphi(v) = \tanh\left(\frac{av}{2}\right)$$

Find asymptotes of functions; what is the value of the function for $v=0$?

Find derivative of function, prove that

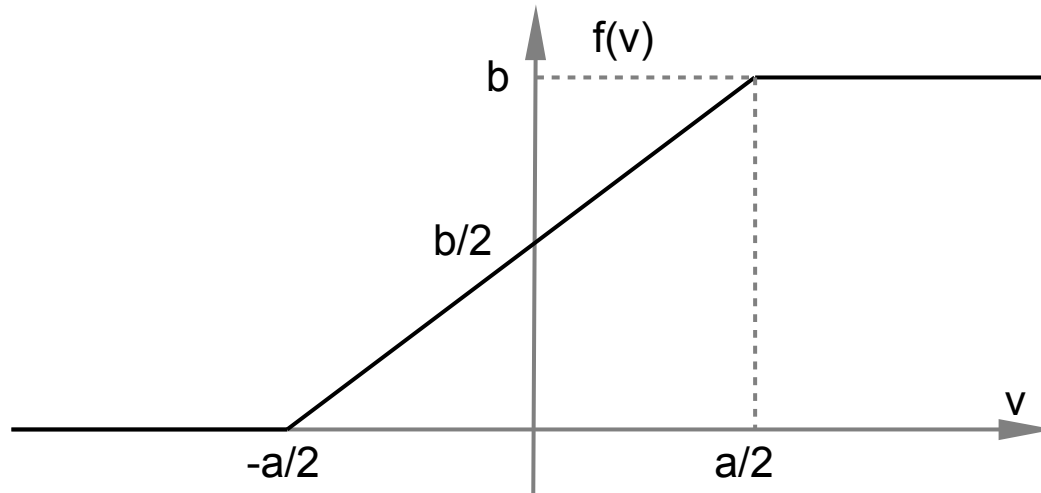
$$\varphi'(v) = \frac{d\varphi(v)}{dv} = \frac{a}{2} [1 - \varphi^2(v)]$$

What is the value of $\varphi'(0)$?

Draw a graph of the function

Exercise 1.3

Write the equation of the function shown in figure.
What equation is when 'a' goes to zero.



Exercise 1.4

Single neuron receives input signals from 4 different synapses. The values of this signals are $\underline{x}=[10, -20, 4, -2]^T$.

Synaptic weights are $\underline{w}=[0.8, 0.2, -1, -0.9]^T$. Calculate the output signal of the neuron to assume a threshold signal (bias) equal to 0. The calculations will be made for three different activation signal:

- a) Linear function;
- b) Step function;
- c) Unipolar sigmoidal function wher $a=1$.

Exercise 1.5

Sketch a multi-layer feedforward networks with all the connections and weights different from zero.

The network consists of:

- 10 inputs signal,
- 2 hidden layers (the first has 4 neurons, the other has 3 neurons),
- single output neuron.

What are the dimensions of each matrix weights?