



POLITECHNIKA POZNAŃSKA

Poznan University of Technology

Introduction to Artificial Intelligence

Theory and algorithms

Dariusz Brzezinski

Agenda

- AI and ML definitions
- Basic machine learning algorithms
 - Linear and logistic regression
 - K-nearest neighbors
 - K-Means
 - Decision trees
 - Naive Bayes
 - Neural Networks
- Explainability



What is Artificial Intelligence (AI)?

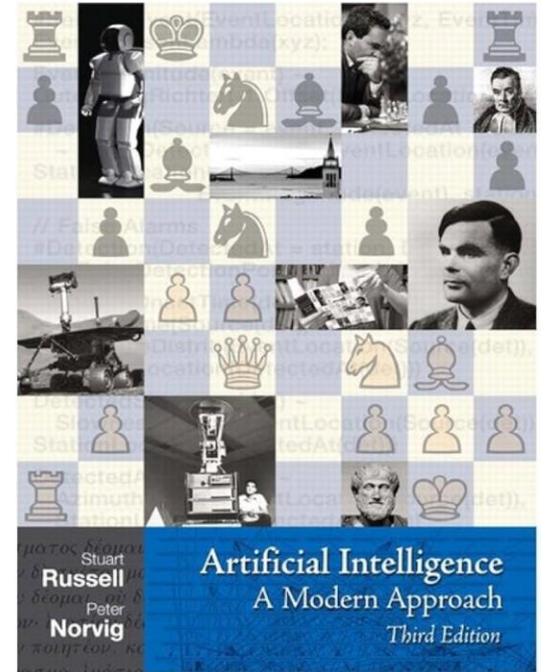
- *The science and engineering of making **intelligent machines** (McCarthy)*
- *The theory and development of computer **systems able to perform tasks normally requiring human intelligence**, such as visual perception, speech recognition, decision-making, and translation between languages (Oxford dictionary)*
- *Field of science dealing with **solving non-algorithmizable problems** (Duch)*

Which intelligence?

- Human intelligence is a broad term encompassing
 - associations, metaphors, and analogies
 - common sense
 - conceptual frameworks
 - creativity
 - empathy
 - ...
- Some research promote the terms **Machine Intelligence** and **Computational Intelligence**

Definition of AI

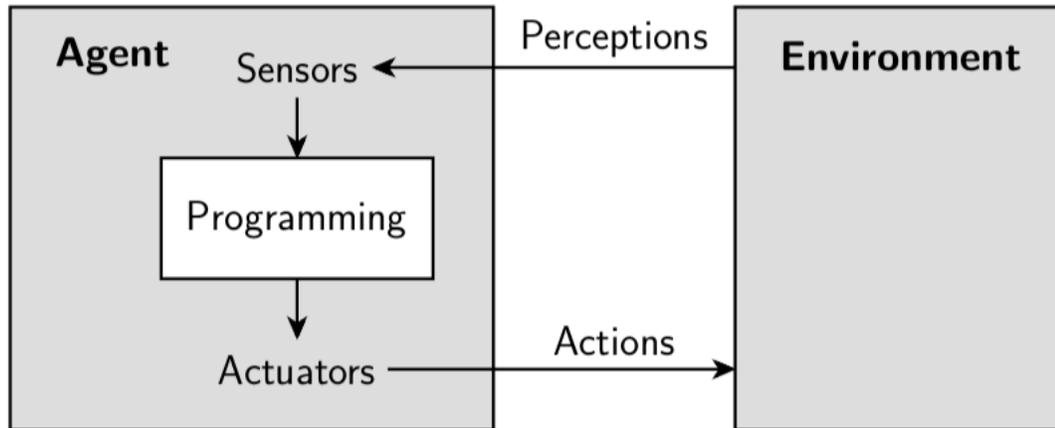
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 - ...
- Some research promote the terms **Machine Intelligence** and **Computational Intelligence**
- Russell and Norvig agree that AI must be defined in terms of *acting* and not *thinking*. They promote the concept of an **intelligent agent**.



Intelligent behavior

- Act rationally to optimize some goals
- Apply knowledge to solve current situation
- Handle complex problems
- Manage missing or uncertain data
- Process and manipulate symbols
- Learn from experiences and surroundings
- Adapt to new situations and tasks

Intelligent behavior



An **agent** perceives its environment through **sensors** and **acts** on the environment through **actuators**.

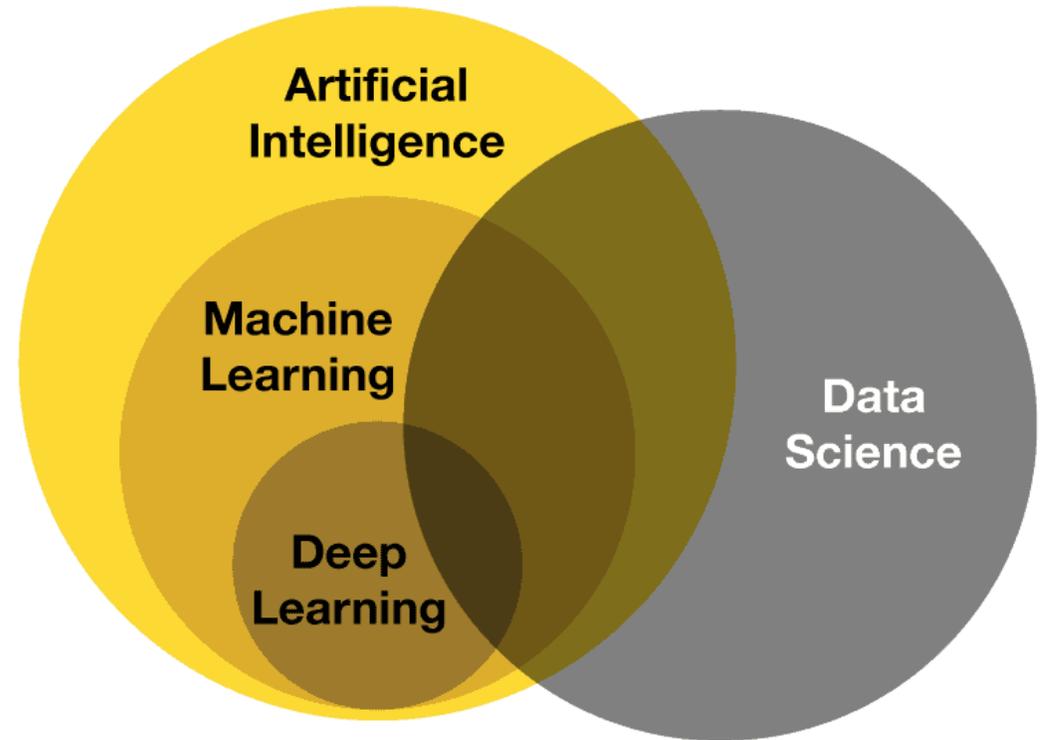
	Human	Robot
Sensors	Eyes, ears, nose, ...	Cameras, mics, lidars, ...
Actuators	Hands, legs, mouth, ...	Grippers, motors, speaker, ...

Different levels of AI

- (Narrow) Artificial Intelligence
 - Intelligent systems for specialized tasks (e.g., speech recognition, image recognition, sentiment analysis, predicting loan risk, planning robot moves)
 - Rational agents that work without figuring out how human reasoning works
- Artificial General Intelligence
 - broadly intelligent, context-aware machines solving general problems
- Superintelligence
 - would outperform humans at nearly every thinking task

Back to our terminological confusion

- Artificial intelligence (AI, AGI)
- **Machine learning (ML)**
- Deep learning (DL)
- Data mining
- Knowledge discovery
- Data science
- Big data
- Statistical data analysis



Machine learning

***Machine learning** is a subfield of artificial intelligence dedicated to algorithms that improve themselves and make predictions based on data. The term is often used interchangeably with artificial intelligence.*

Various applications:

- Internet search engines
- Recommendation systems
- Face recognition
- Voice recognition
- Spam filtering
- Credit risk assessment

When to use machine learning?

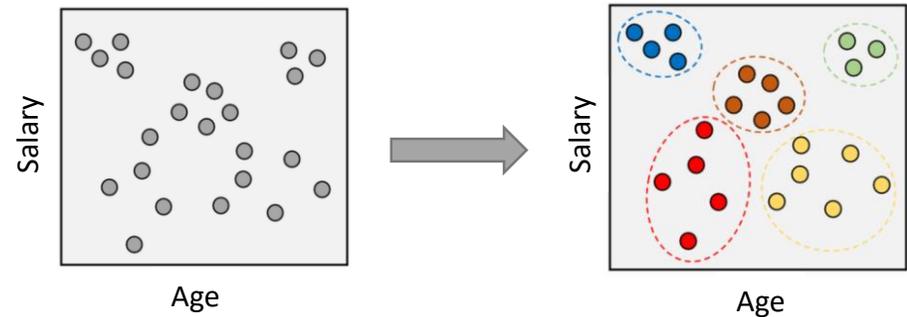
- 1. There is a pattern in the studied problem**
- 2. We cannot model the pattern mathematically***
- 3. We have data on the problem**

Yaser Abu-Mostafa
Learning from Data

Machine learning

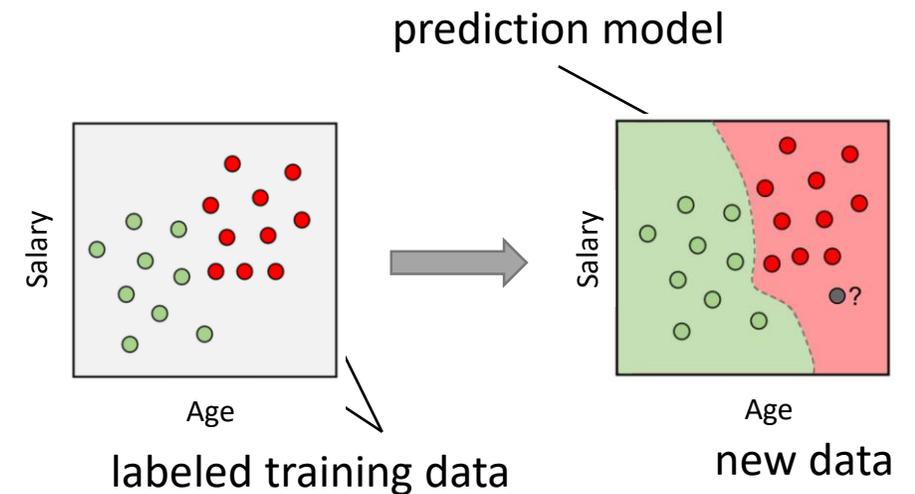
- **Unsupervised** (without a teacher)

- Clustering
- Association mining



- **Supervised** (with a teacher)

- Classification
- Regression
- Reinforcement learning



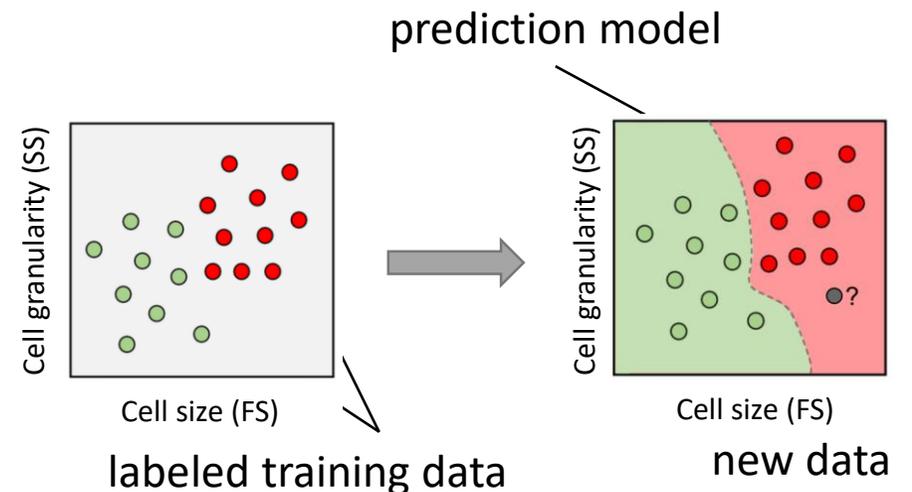
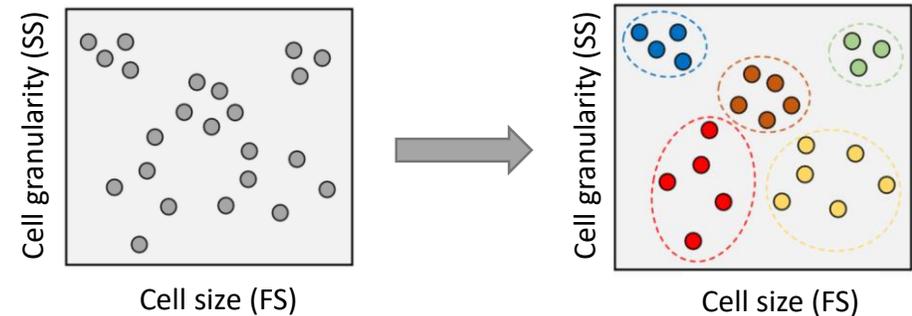
Machine learning

- **Unsupervised** (without a teacher)

- Clustering
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- **Supervised** (with a teacher)

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- Regression
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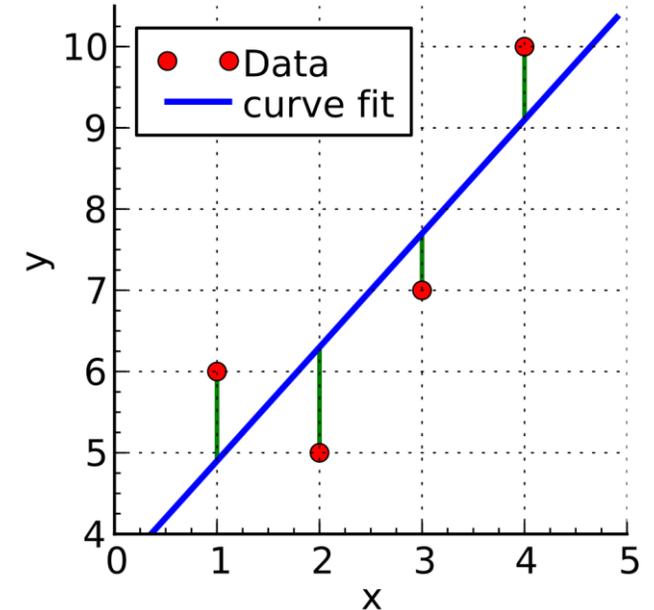
But how do you create a prediction model?

Prediction model = ML Algorithm + Hyperparameters + Data

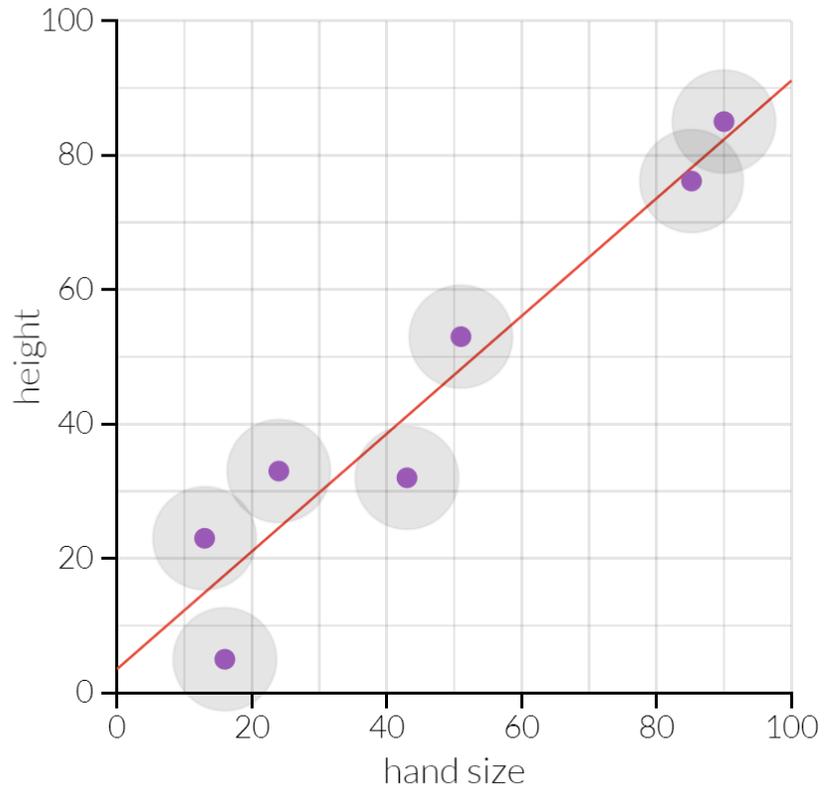
- **Algorithms discover patterns** in data and generalize them
- Algorithms usually have **hyperparameters** that **have to be tuned**
- **You always need** some form of **data**
- Many approaches:
 - Probabilistic models (bayesian methods)
 - Distance-based learning (nearest neighbors)
 - Symbolic learning (trees, rules)
 - Function approximation (regression, neural nets)

Linear regression

- Simple model for predicting continuous values
- General idea: Fit a line to the data to minimize average error
- What kind of error?
 - Typically mean squared error (L2, OLS)
 - Could be mean absolute error (L1, quantile regression)
 - Huber loss (robust regression)
- Commonly used in medicine
- Interpretable results: $y = b_0 + b_1x_1 + \dots$



Linear regression



Beta 1 - The y-intercept of the regression line.

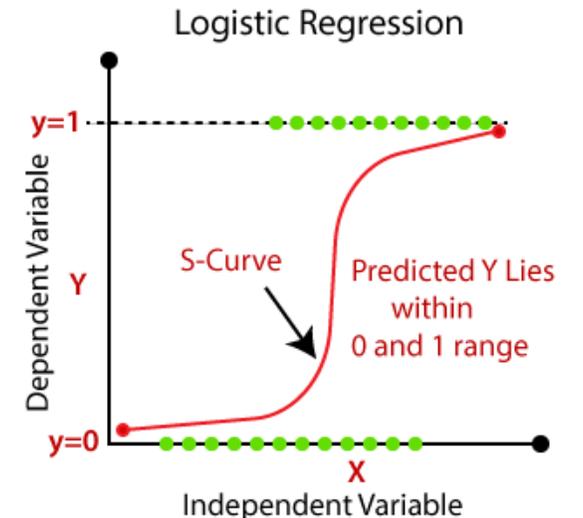
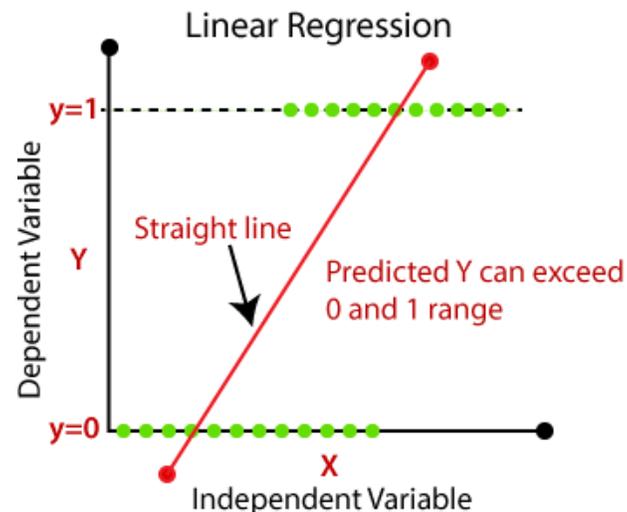
$$3.46 + 0.88 * \text{hand size} = \text{height}$$

Beta 2 - The slope of the regression line.

<https://setosa.io/ev/ordinary-least-squares-regression/>

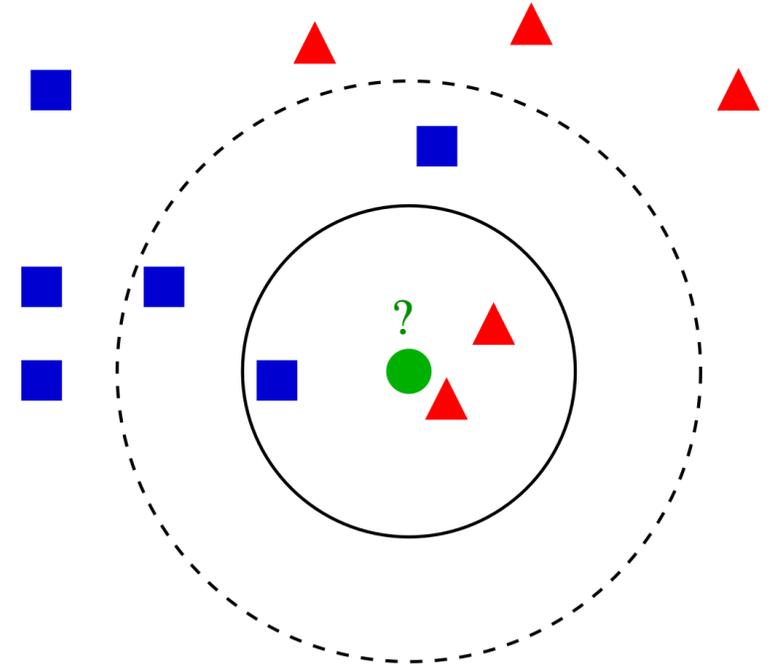
Logistic regression

- Linear model for predicting categorical values
- Sigmoid function instead of linear function
- Returns values from 0 to 1
- Interpretable model
- $\log(y/(1-y)) = b_0 + b_1x_1 + \dots$



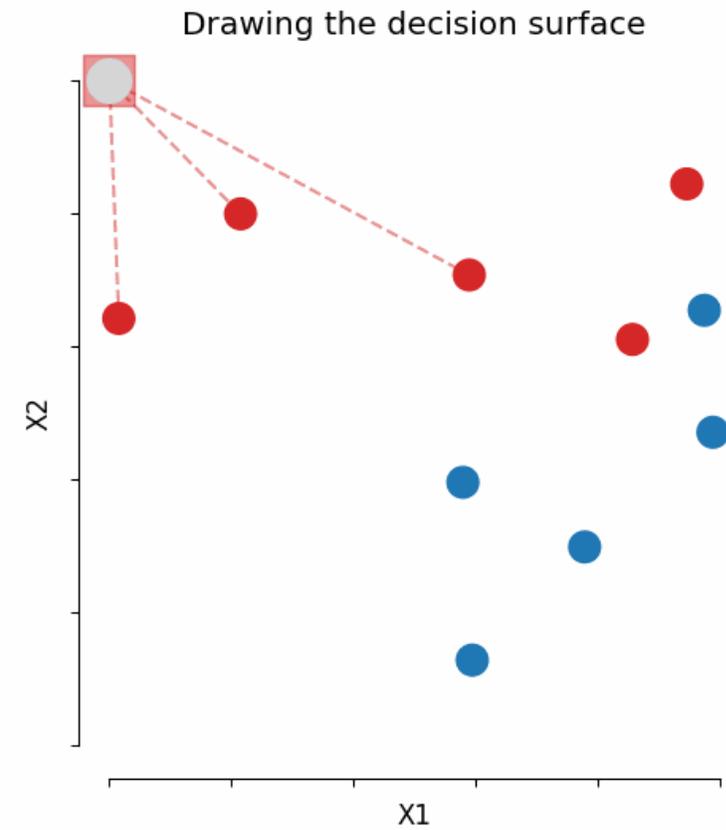
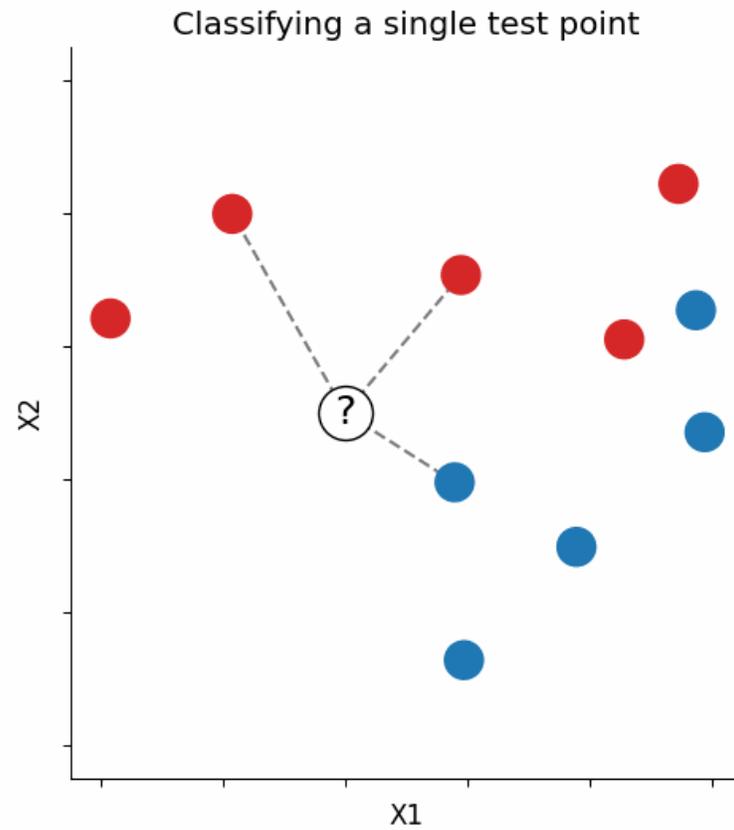
K-nearest neighbors

- Predictions based on similarity
- Base prediction on the most class common class of k nearest neighbors
- For regression average target values of k nearest neighbors
- Requires storing the training data
- k is a hyperparameter
- Needs a distance function
- All attributes must be on the same scale!



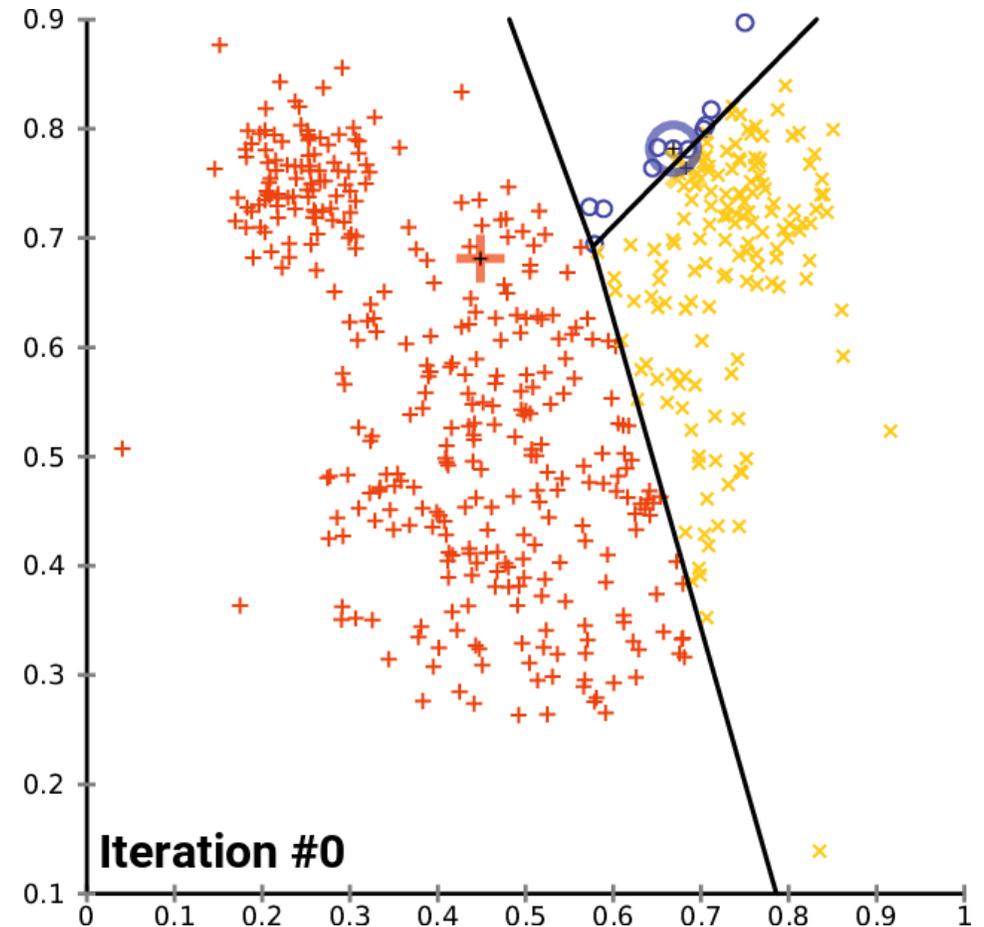
K-nearest neighbors

kNN classifier | $k = 3$



K-means

- Distance based approaches are also used for **clustering**
- Clustering = similar examples should be in the same cluster, dissimilar in different clusters
- K-means is an algorithm that finds k clusters that minimize the sum of squared within cluster distances
- All attributes must be on the same scale!

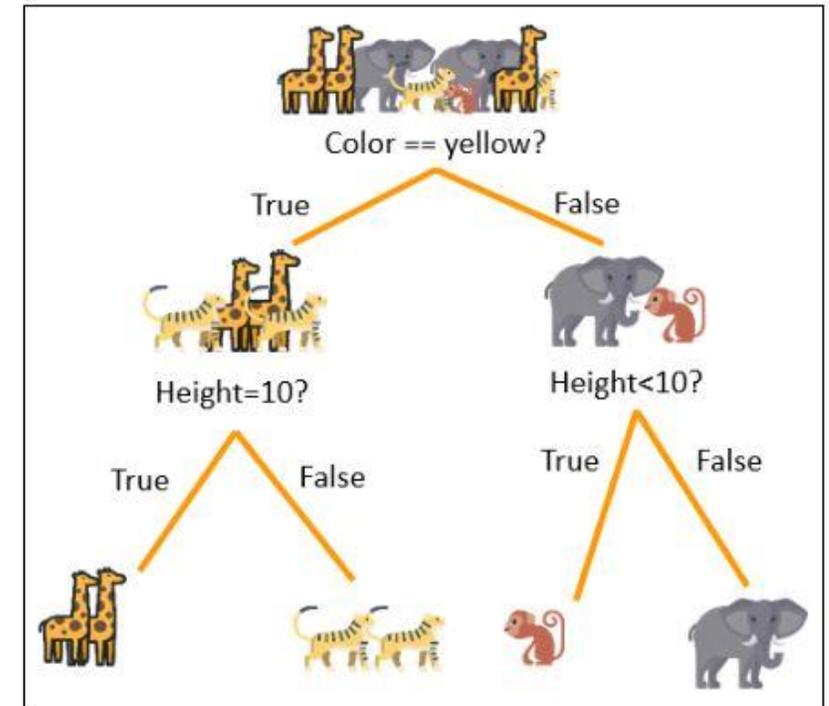


Decision trees

Representing knowledge as a tree:

- Each internal node tests an attribute
- Each branch corresponds to an attribute value
- Each leaf node assigns a classification

Training Dataset		
Color	Height	Label
Grey	10	Elephant
Yellow	10	Giraffe
Brown	3	Monkey
Grey	10	Elephant
Yellow	4	Tiger



Decision trees

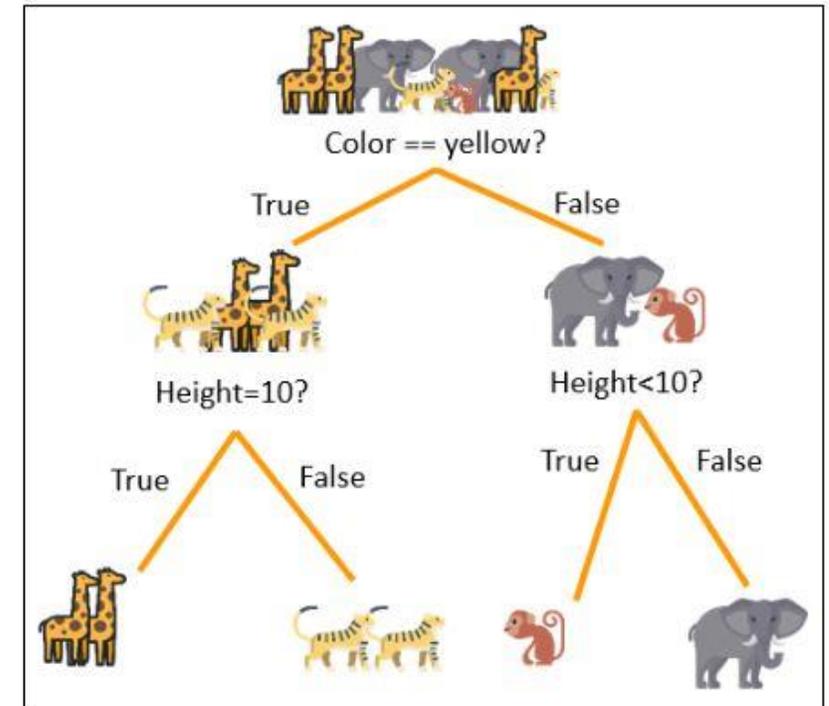
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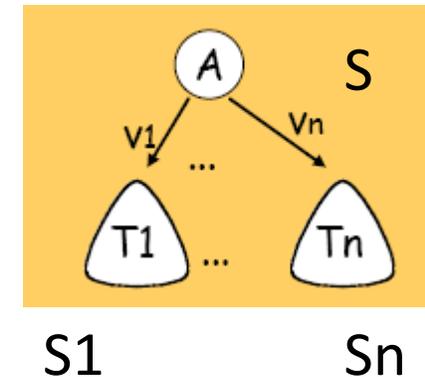


Decision trees

- Decision trees are created in (recursive) steps
- At start, all training examples S are at the root of the tree.
- **If** all examples from S belong to the same class K_j
then label the node / leaf with K_j

else

- select the „best” attribute A
- divide S into S_1, \dots, S_n according to values v_1, \dots, v_n of attribute A
- Recursively build subtrees T_1, \dots, T_n for S_1, \dots, S_n
- Stop if all nodes are labeled leaves



Decision trees

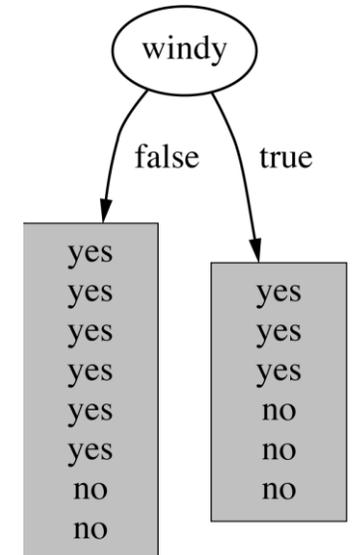
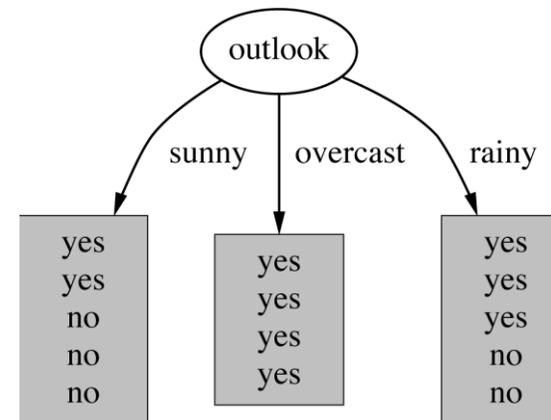
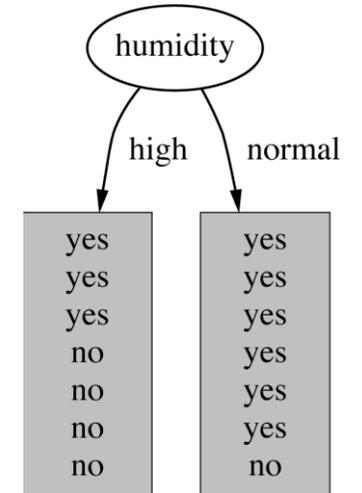
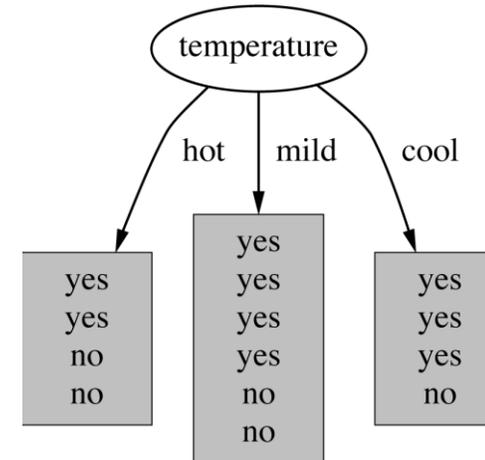
- Example dataset: Golf (Play or not?)

Outlook	Temperature	Humidity	Windy	Play?
sunny	hot	high	false	No
sunny	hot	high	true	No
overcast	hot	high	false	Yes
rain	mild	high	false	Yes
rain	cool	normal	false	Yes
rain	cool	normal	true	No
overcast	cool	normal	true	Yes
sunny	mild	high	false	No
sunny	cool	normal	false	Yes
rain	mild	normal	false	Yes
sunny	mild	normal	true	Yes
overcast	mild	high	true	Yes
overcast	hot	normal	false	Yes
rain	mild	high	true	No



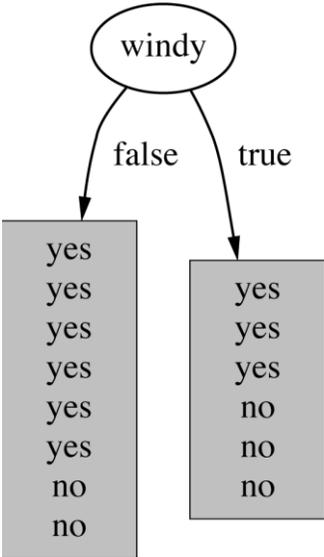
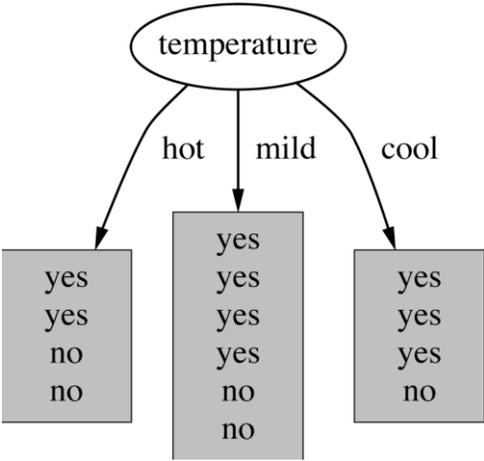
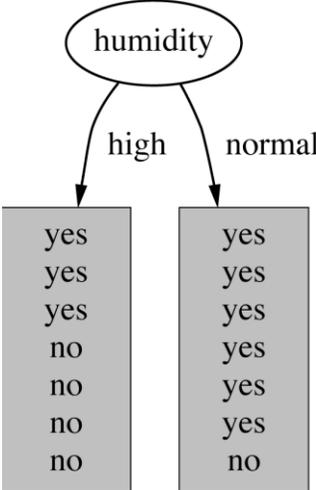
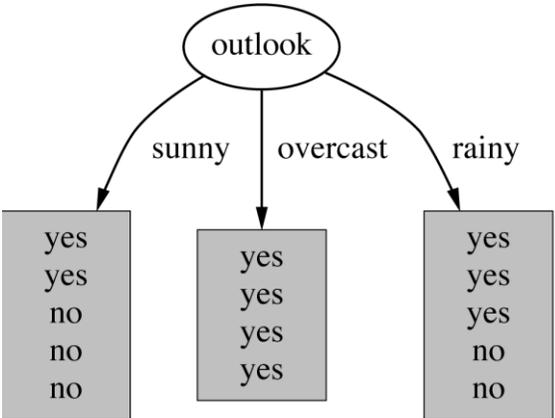
Decision trees

- Example dataset: Golf (Play or not?)
- What constitutes a good split?



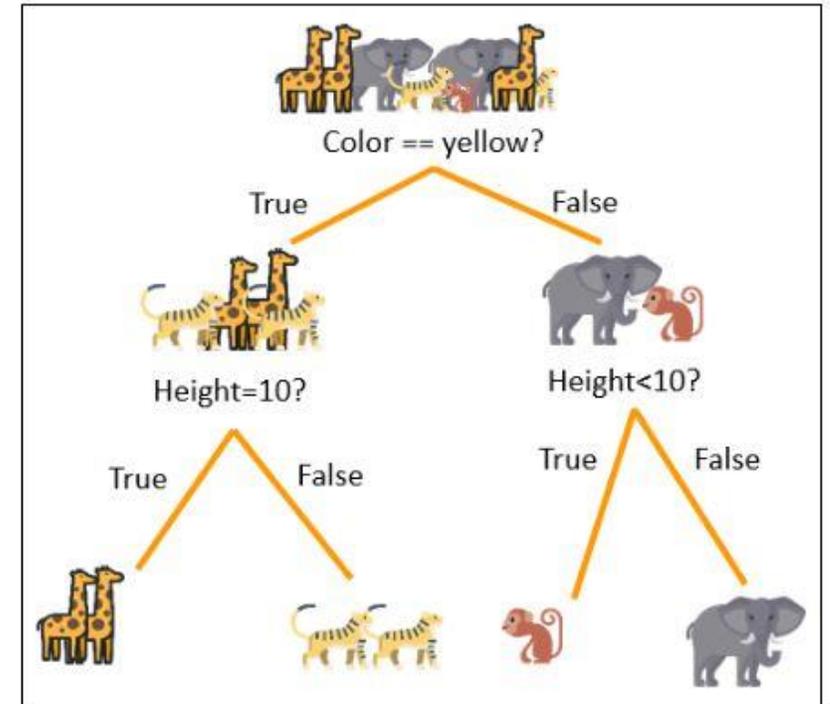
Decision trees

- Example dataset: Golf (Play or not?)
- What constitutes a good split?
- $Entropy(S) = -\sum_{i=1..n} p_i * \log_2 p_i$
- $Entropy(S,A) = \sum_{j=1..k} |S_j| / |S| * Ent(S_j)$
- $InfoGain(S,A) = Ent(S) - Ent(S|A)$
- $InfoGainRatio(S,A) = InfoGain(S,A) / Ent(A)$



Rules

- Decision trees can be read as rules
- Decision rules:
IF *Conditions* THEN *Class*
- One needs lists of rules to apply
- Dedicated algorithms in addition to tree interpretations
- Rules can also be created based on associations



Association rules

- Market basket analysis
- {Cereal, Milk} → Bread [sup=5%, conf=80%]
- *80% of customers who buy cereal and milk also buy bread and 5% of customers buy all these products together*
- Applications
 - Product placement in stores
 - Recommender systems
 - Rule discovery in life sciences

TID	Produce
1	MILK, BREAD, EGGS
2	BREAD, SUGAR
3	BREAD, CEREAL
4	MILK, BREAD, SUGAR
5	MILK, CEREAL
6	BREAD, CEREAL
7	MILK, CEREAL
8	MILK, BREAD, CEREAL, EGGS
9	MILK, BREAD, CEREAL

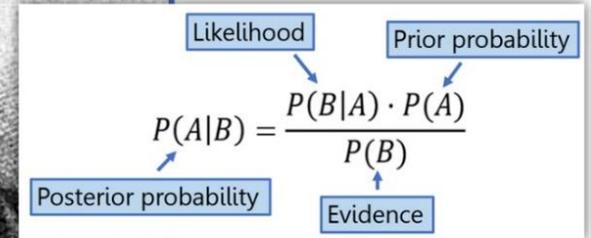
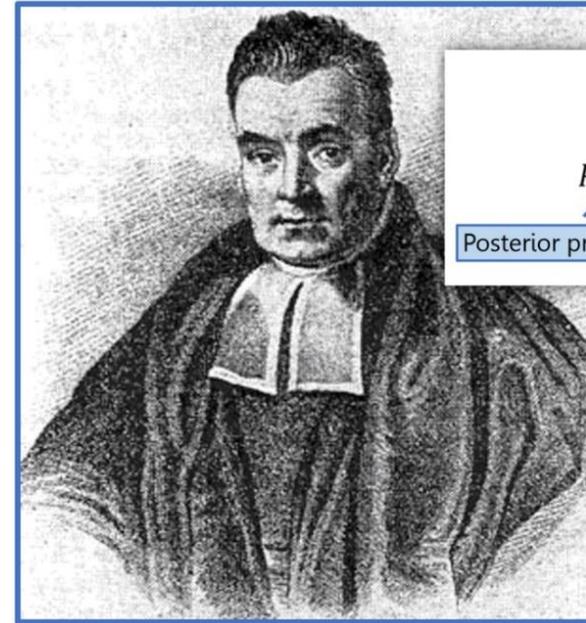
Bayesian theorem

- Given training data X , posteriori probability of a class C , $P(C|X)$ follows the Bayes theorem

$$P(C|X) = \frac{P(X \wedge C)}{P(X)} = \frac{P(X|C)P(C)}{P(X)}$$

- Maximum posteriori (MAP):
 - Choose the most probable hypothesis under the given conditions

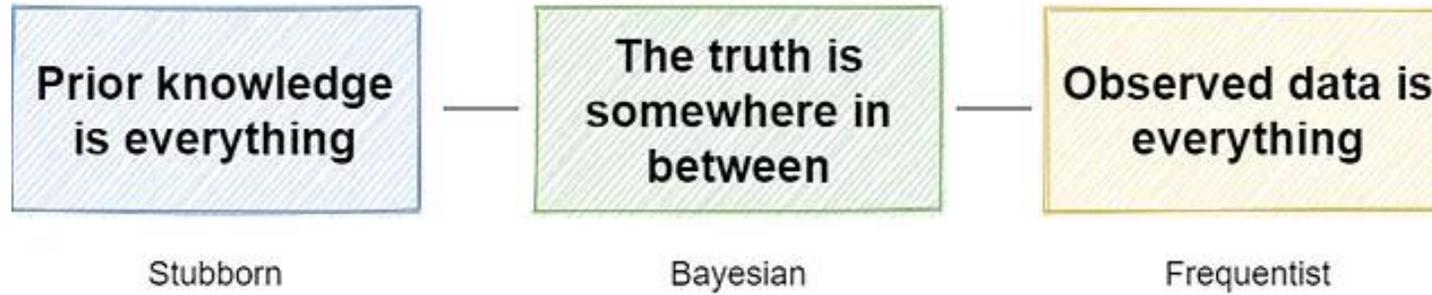
$$C_{MAP} = \arg \max_{C_i \in CD} P(C = C_i)P(X|C = C_i)$$



Thomas Bayes

Bayesian models

Points of View



Naive Bayes classifier

- Assume conditional independence of attribute values

$$P(X|C = C_i) = \prod_{j=1}^m P(A_j = x_j|C = C_i)$$

where $X = (A_1 = x_1, A_2 = x_2, \dots, A_m = x_m)$

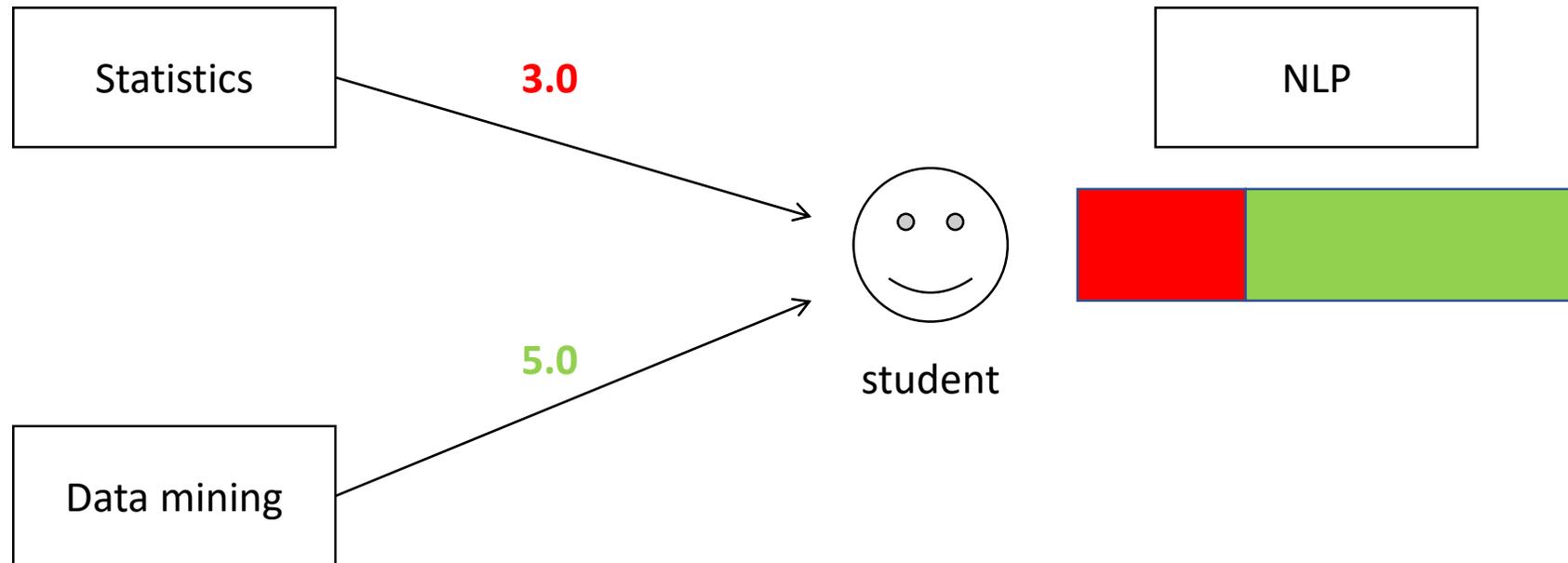
- Following the MAP approach we get

$$C_{MAP} = \arg \max_{C_i \in CD} P(C = C_i) \prod_{j=1}^m P(A_j = x_j|C = C_i)$$

- Now probabilities can be estimated by counts

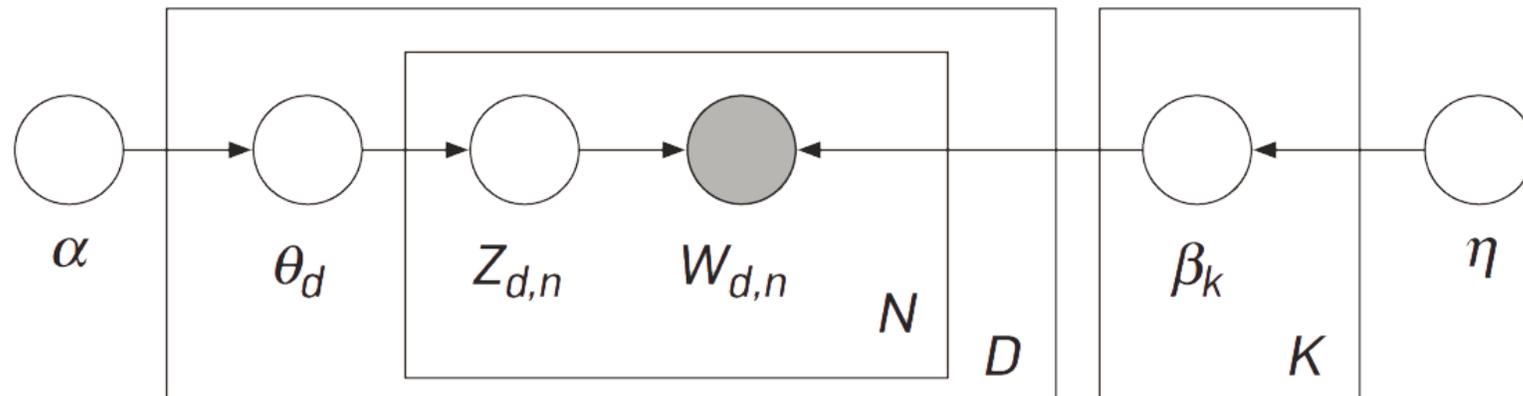
$$P(C = C_i) = \frac{s_i}{N} \text{ and } P(A_j = x_j|C = C_i) = \frac{s_{ij}}{s_i}$$

Bayesian networks

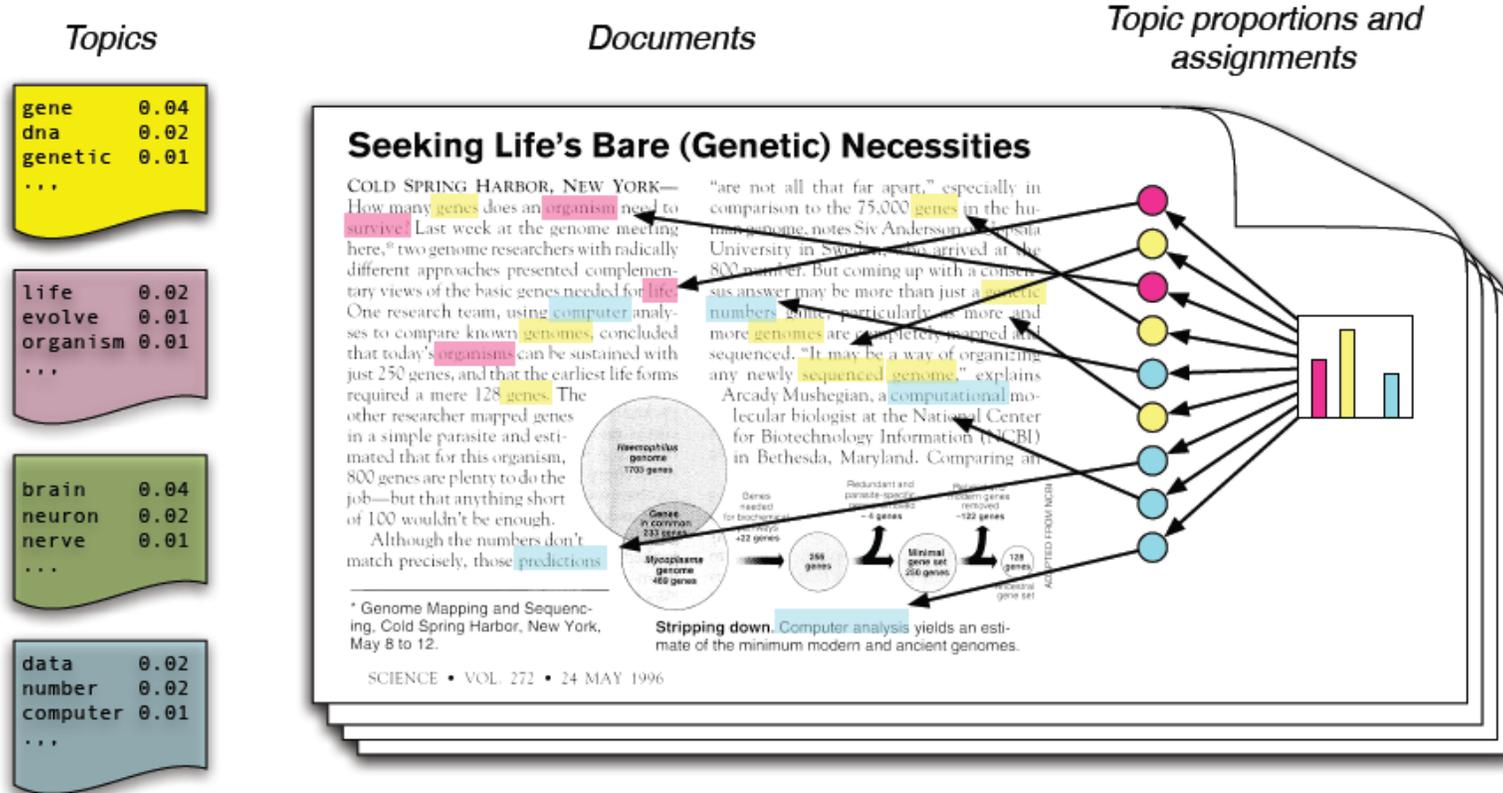


Bayesian networks (topic modeling)

$$= \prod_{i=1}^K p(\beta_i) \prod_{d=1}^D p(\theta_d) \left(\prod_{n=1}^N p(z_{d,n} | \theta_d) p(w_{d,n} | \beta_{1:K}, z_{d,n}) \right)$$

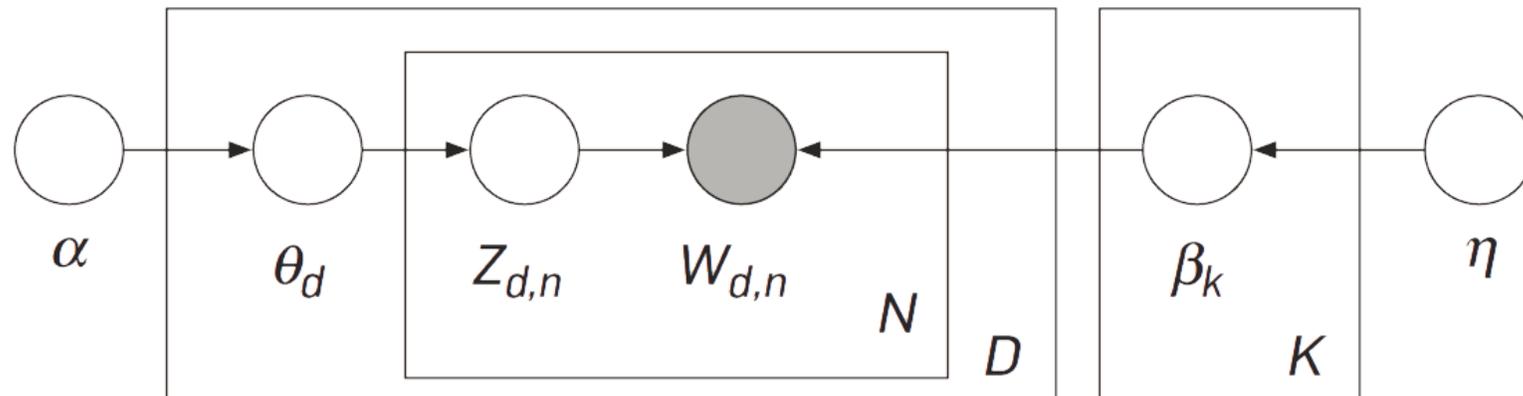


Bayesian networks (topic modeling)



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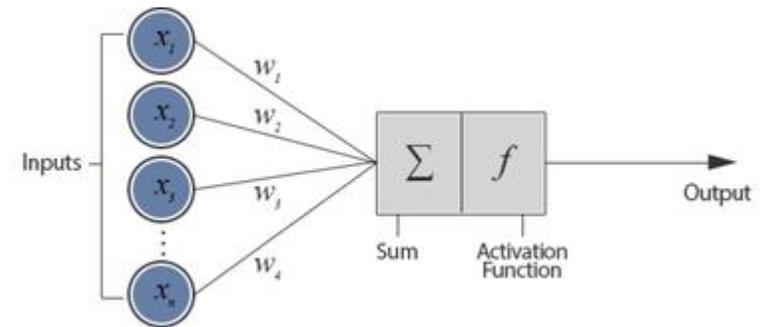
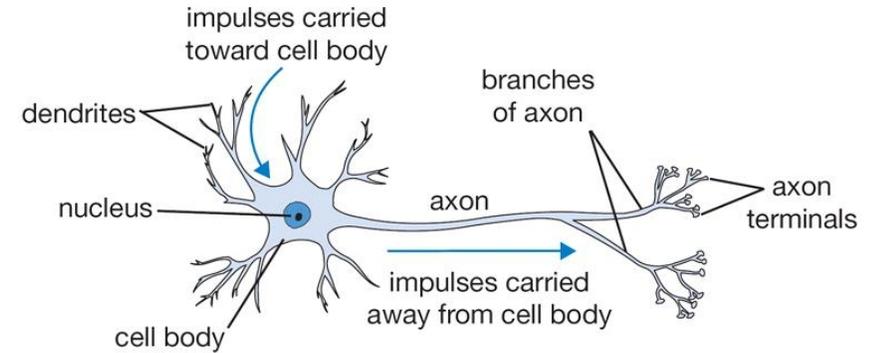
Artificial Neural Networks (ANN)

- A neural network is a machine learning algorithm
- The basic idea of training on data is the same as in decision trees or k-NN
- The main difference is the modularity
- To train a neural network you have to define:
 - **Architecture** (number, type, and arrangement of neurons)
 - **Loss function** (what we optimize)
 - **Optimizer** (algorithm that steer the training)
- If you define the above, you can use the net as any other classifier



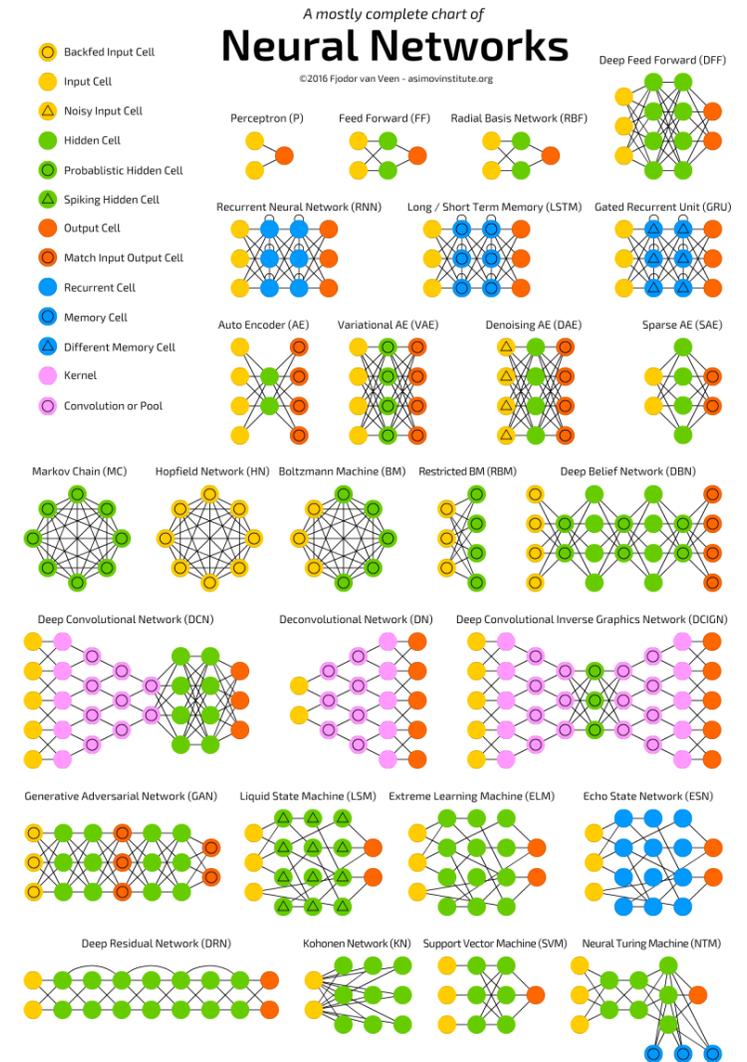
Architecture

- The basic building block of ANN is a **neuron**
- An artificial neuron is a signal processor:
 - Vector of numbers as **input**
 - Each input is multiplied by a **weight** and summed into an **activation**
 - The activation is then transformed by a (non-linear) **activation function**
 - **Outputs** the result



Architecture

- The architecture defines the tasks the neural network can solve
- A good neural network architecture can transform raw data into features
- Representation learning
- End-to-end learning
- People reuse architectures from others to solve their own problems



Loss function

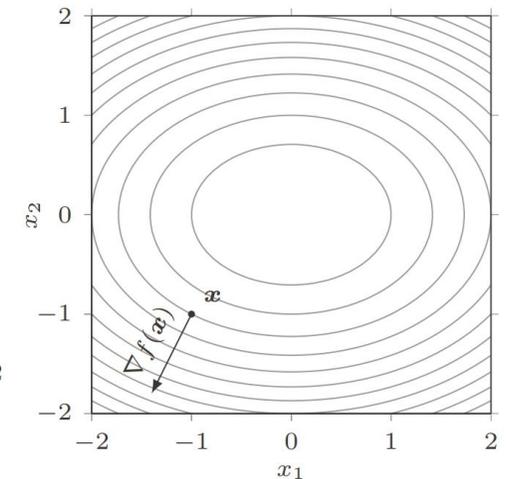
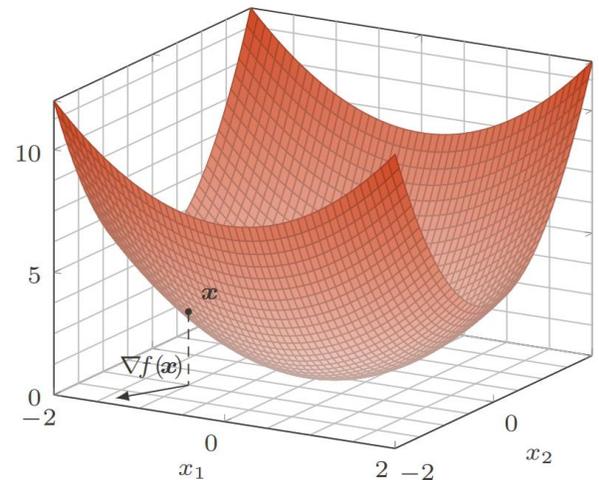
- Loss functions have to be differentiable
- Typical loss function:
 - **MAE, MSE, MAPE**
 - For regression
 - **Categorical cross entropy** (aka softmax)
 - Combined with softmax activation (activation on an entire vector (sic!) of numbers)
 - Class probabilities sum up to 1
 - **Binary cross entropy** (aka sigmoid)
 - For multilabel classification
 - Class probabilities do not have to sum up to 1

Optimizer

- Iteratively updates the input weights

$$\mathbf{x}_{k+1} = \mathbf{x}_k - \alpha_k \nabla f(\mathbf{x}_k)$$

- The loss function's gradient ∇ shows the direction of optimization
- How to define update speed α_k (**learning rate**)
- Multiple heuristics:
 - SGD, SGD + Momentum,
 - Adagrad, RMSprop,
 - Adam, Adadelta

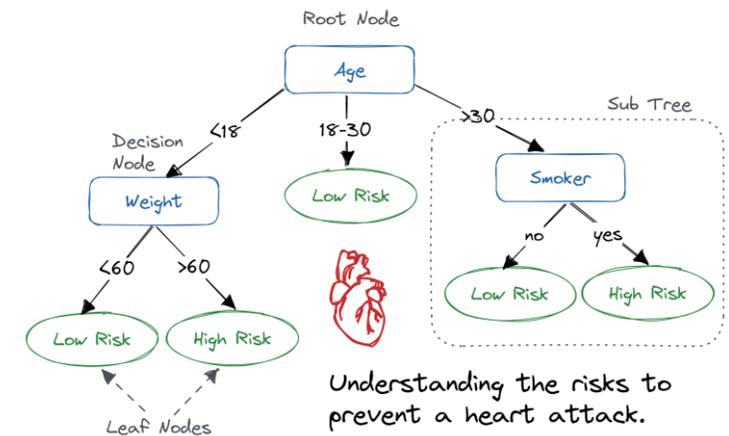


Explainability

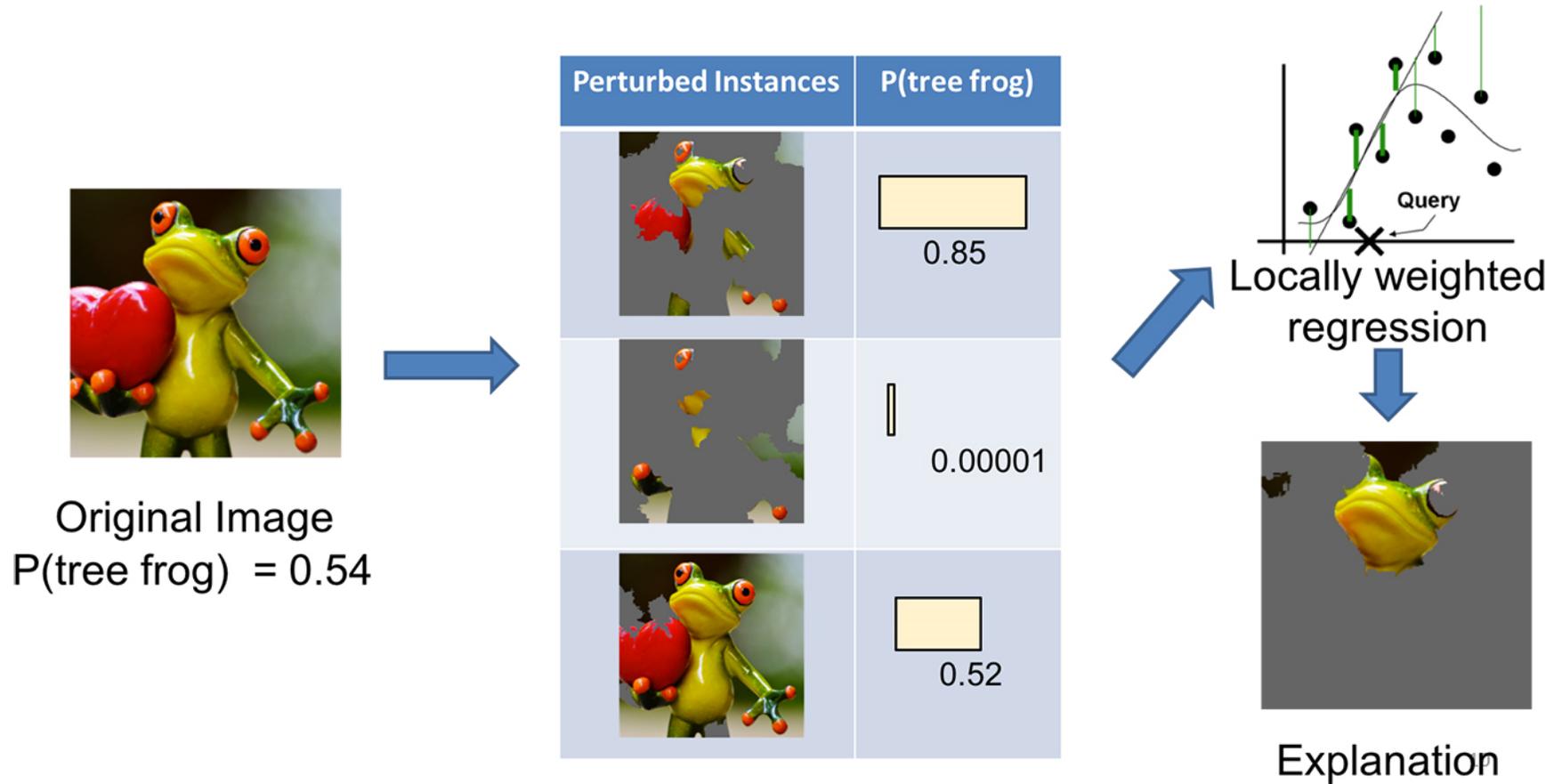
- Good predictive performance is not everything
- Many machine learning models are **black boxes**
- When using AI systems that impact our lives **we want to be able to explain model predictions**
 - Bank loans
 - Court case management
 - Medical diagnoses
 - Treatment selection

Explainability

- Some models (e.g. rules or decision trees) are interpretable by nature
- In recent years, several model agnostic explainability algorithms have been developed, which work for any machine learning model
- General idea: modify (perturb) examples and see how it affects the prediction
- Popular model agnostic methods:
 - LIME
 - SHAP

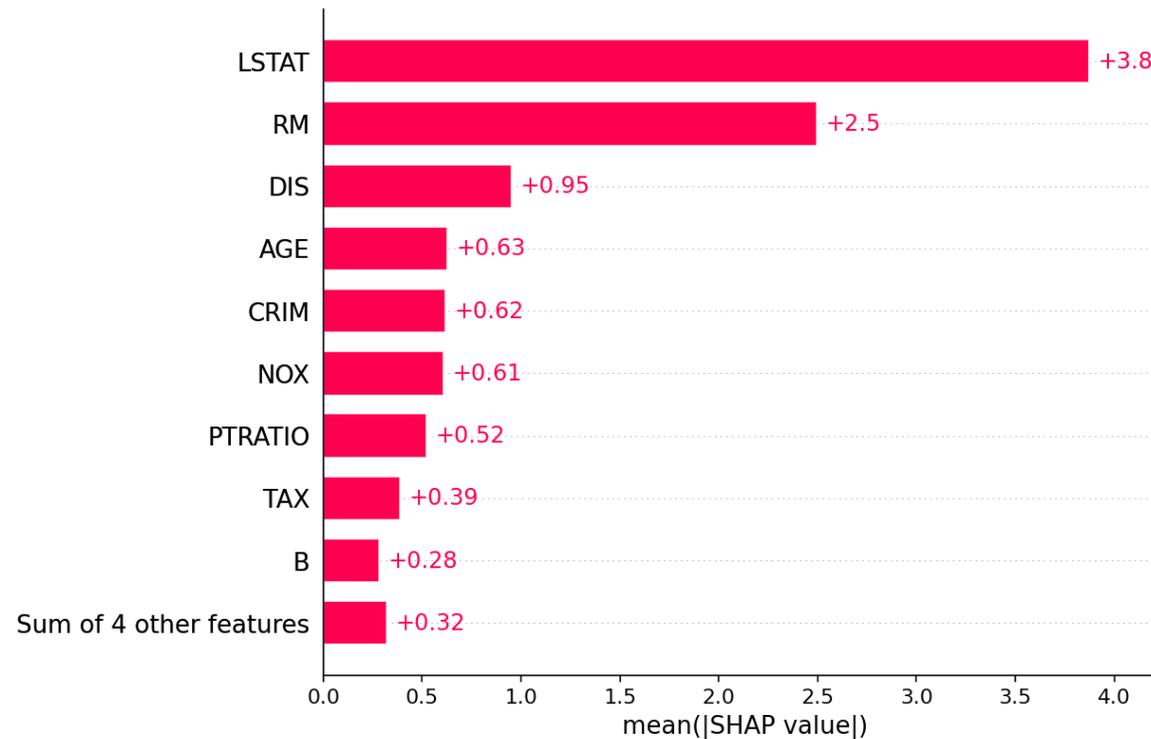


Model agnostic methods (LIME)



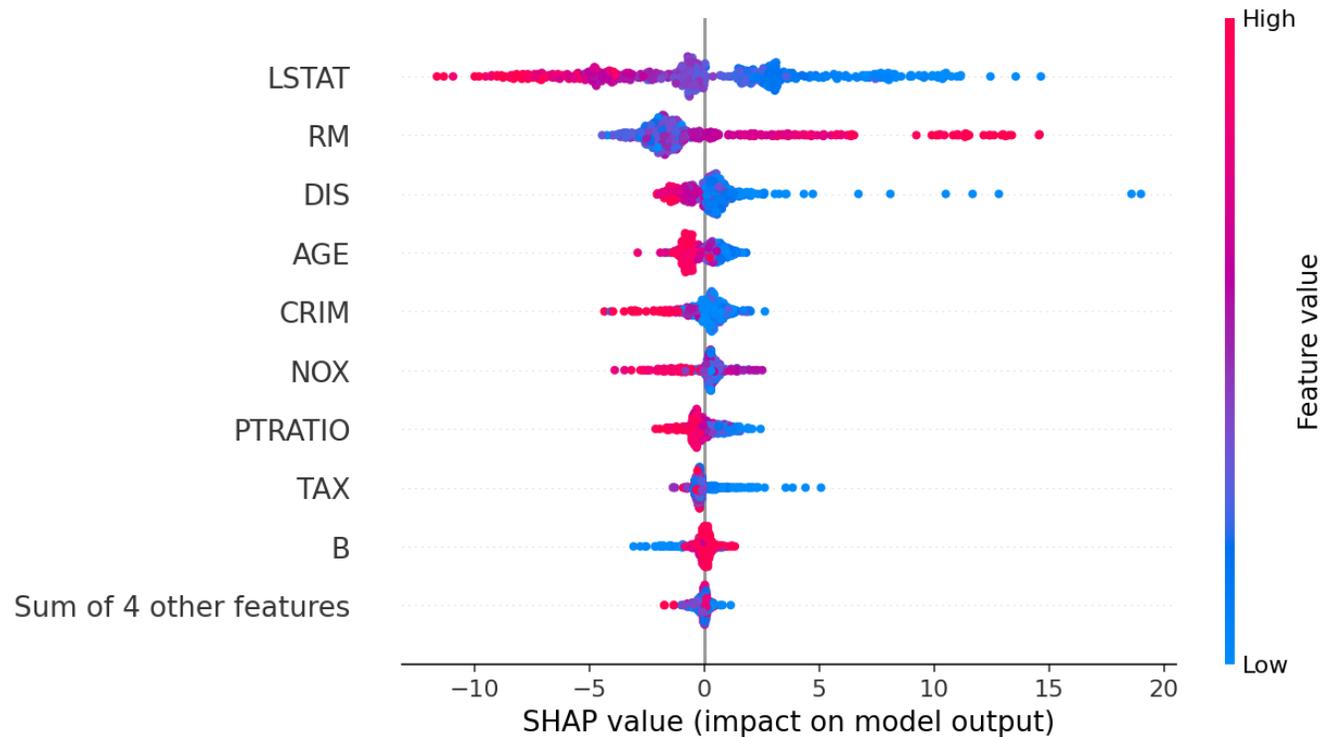
Feature importance plot

Questions answered: *Which features are (on average) the most important when making predictions?*



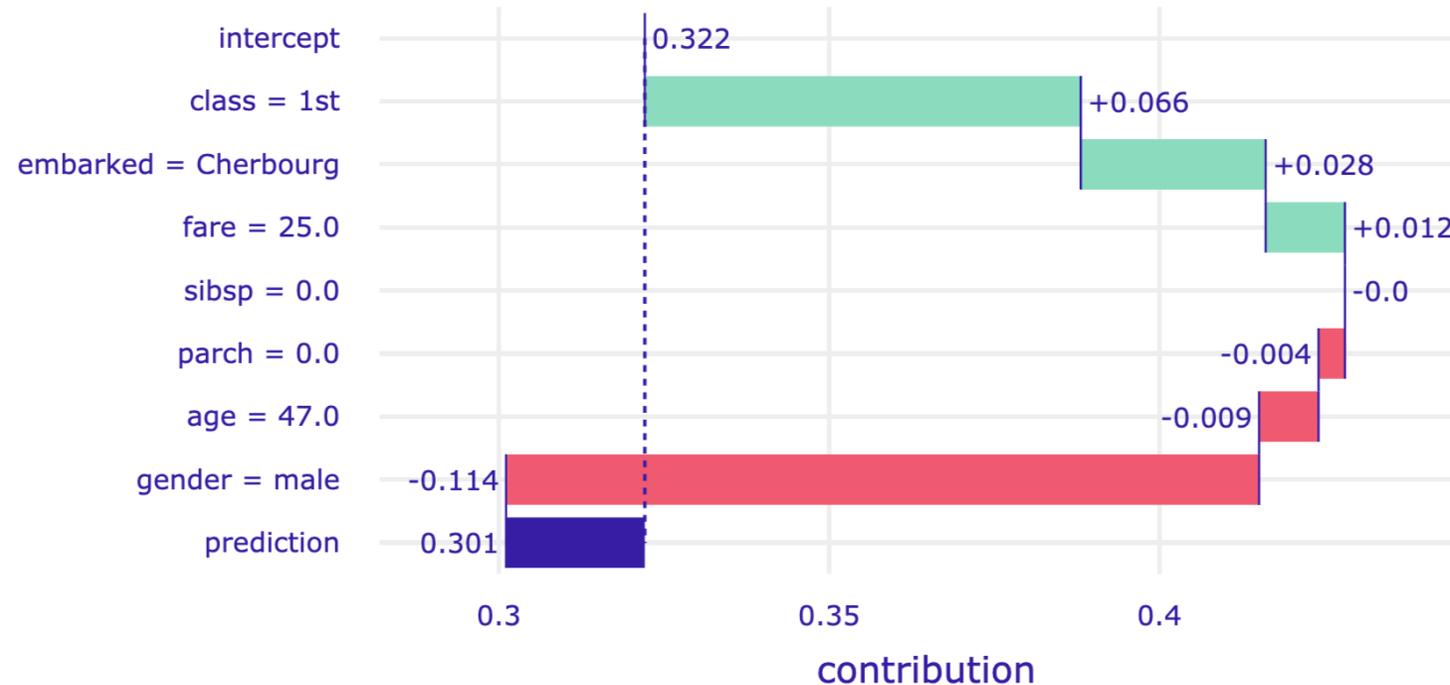
SHAP summaries

Questions answered: *What were the feature importances for each prediction?*



Contribution plots (waterfall chart)

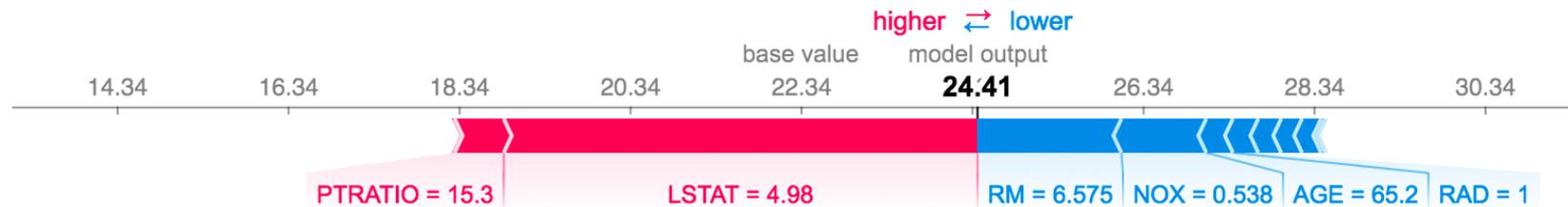
Questions answered: *What contributed to a given prediction?*



Baniecki, H. et al. (2021). Dalex: responsible machine learning with interactive explainability and fairness in python. *Journal of Machine Learning Research*, 22(214), 1-7.

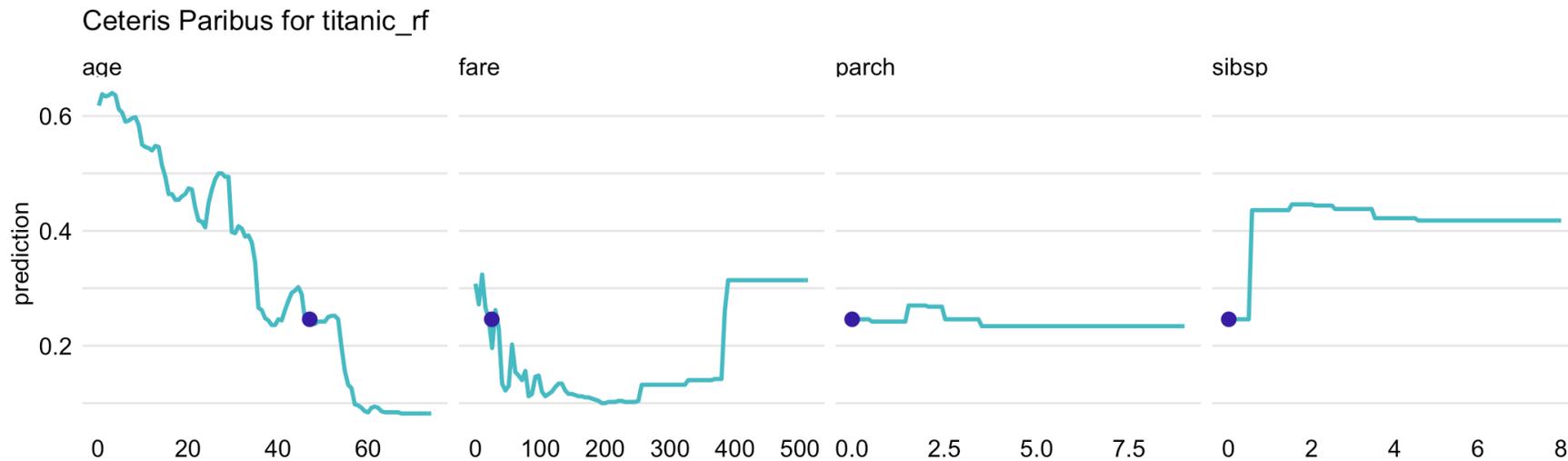
Contribution plots (force plot)

Questions answered: *What contributed to a given prediction?*



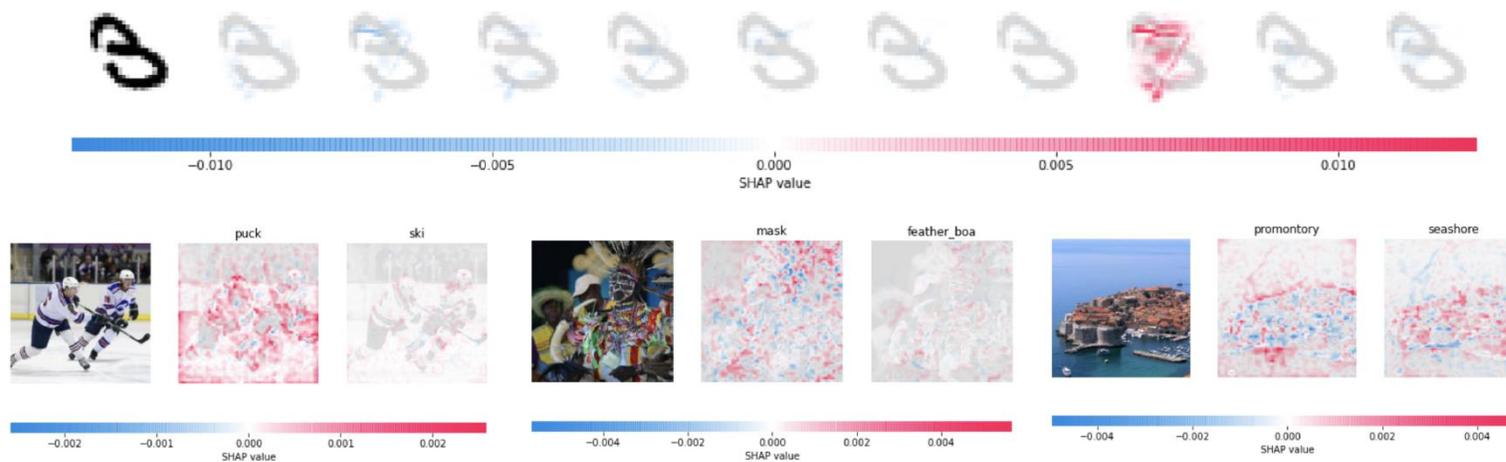
Ceteris paribus profile

Questions answered: *How a change of a feature value would affect a given prediction?*



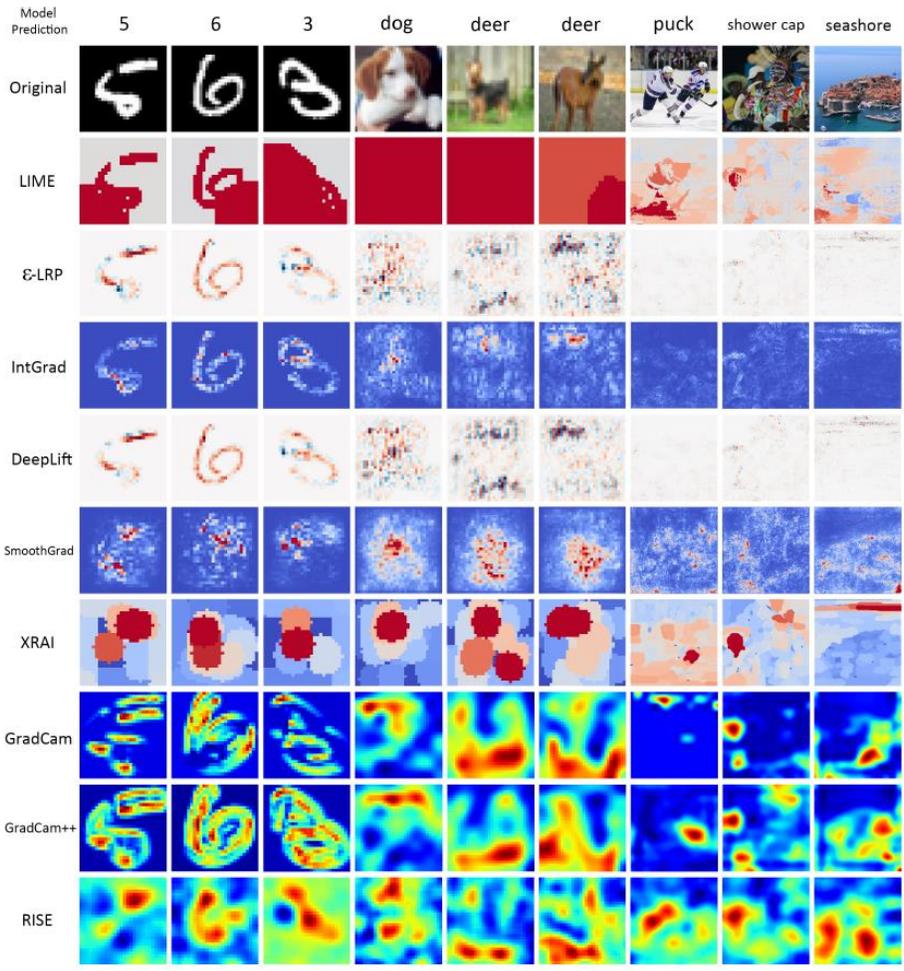
Saliency maps

Question answered: *Which pixels contributed to the prediction?*

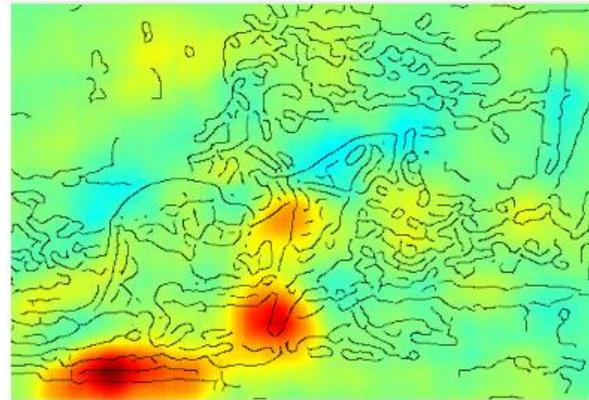


Bodria, F., Giannotti, F., Guidotti, R., Naretto, F., Pedreschi, D., & Rinzivillo, S. (2023). Benchmarking and survey of explanation methods for black box models. *Data Mining and Knowledge Discovery*, 37(5), 1719-1778.

Saliency maps



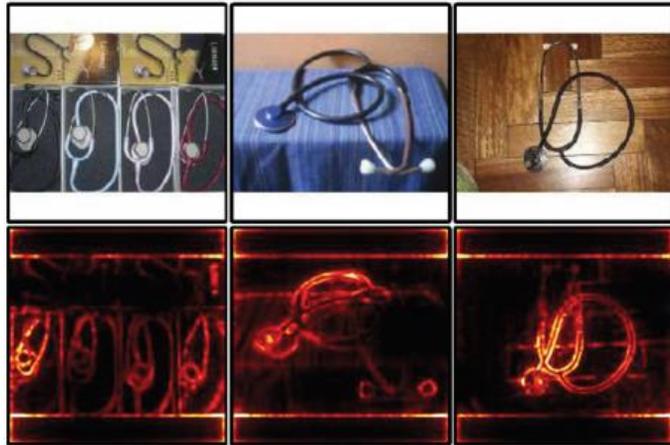
Success stories



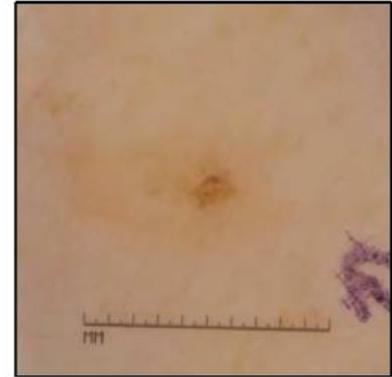
(a) Husky classified as wolf



(b) Explanation

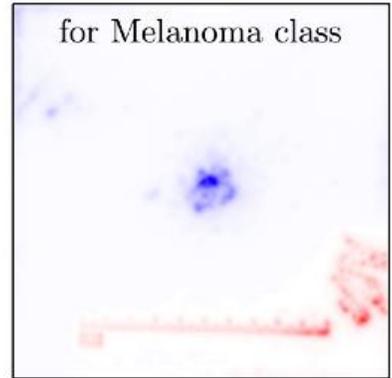


input

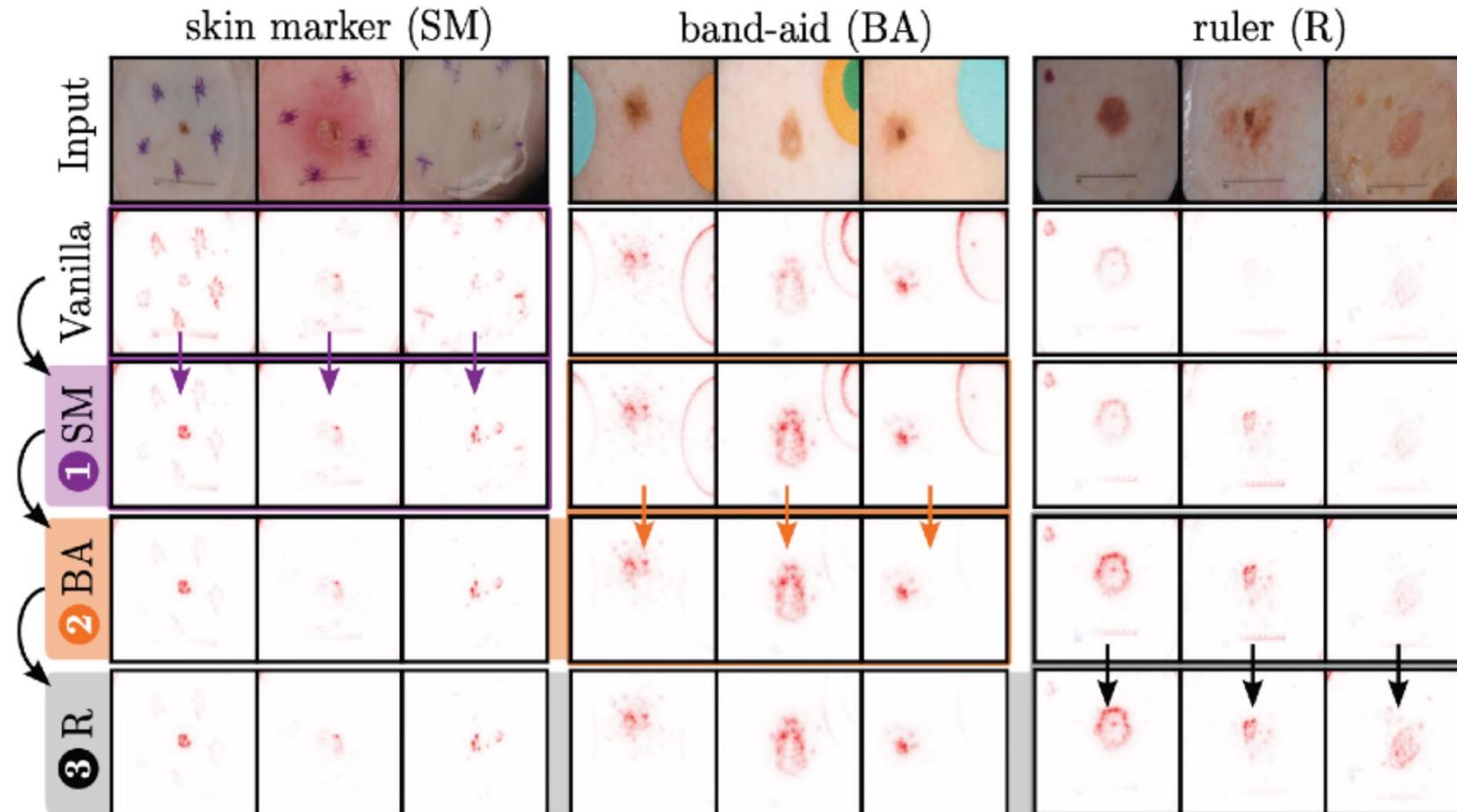


heatmap

for Melanoma class



Related topic: machine unlearning



Pahde, F., Dreyer, M., Samek, W., & Lapuschkin, S. (2023). Reveal to revise: An explainable ai life cycle for iterative bias correction of deep models. In *International Conference on Medical Image Computing and Computer-Assisted Intervention* (pp. 596-606). Cham: Springer Nature Switzerland.

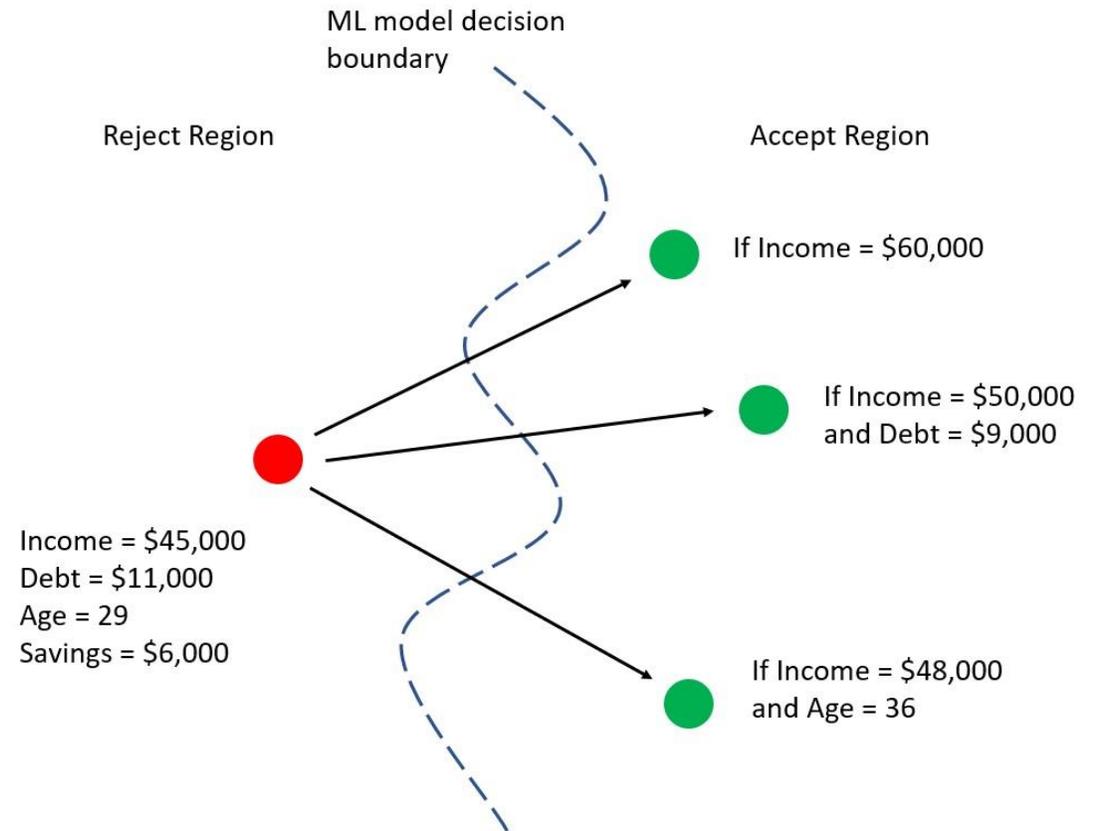
Sentence highlighting

Question answered: *Which words contributed to the prediction?*

INTGRAD	the movie is not that bad , ringo lam sucks . i hate when van dam ##me has love in his movies , van dam ##me is good only when he doesn ' t have love in his movies .
LIME	the movie is not that bad , ringo lam sucks . i hate when van dam ##me has love in his movies , van dam ##me is good only when he doesn ' t have love in his movies .
DeepLift	the movie is not that bad , ringo lam sucks . i hate when van dam ##me has love in his movies , van dam ##me is good only when he doesn ' t have love in his movies .
Gradient x Input	the movie is not that bad , ringo lam sucks . i hate when van dam ##me has love in his movies , van dam ##me is good only when he doesn ' t have love in his movies .

Counterfactual explanations

- **Counterfactual explanations** – describe causal relations between changes in conditions and changes in decisions
- In machine learning – the smallest object modification that changes the prediction
- *If the client earned \$60 000 annually instead of \$45 000, they'd get the loan*



Summary

- **Artificial intelligence** (machine intelligence) is usually defined as **intelligent actions** rather than thinking
- **Machine learning** is the basic building block of AI
- Predictive models are **patterns discovered by algorithms from data**
- Many algorithms for finding patterns (**probability, function approximation, rules, distance**)
- **Explainability** plays an important role in AI applications
- **Explaining model predictions \neq explaining phenomenon**

